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EOMET-77 ATMOSPHERIC TRANSMISSION VALUES DERIVED FROM PHOTOGRAPHS OF THE SEA HORIZON (U)

HSS Inc

2 Alfred Circle

Bedford, Ma 01730

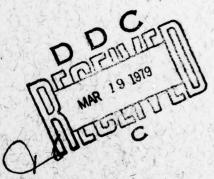
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28 December 1978

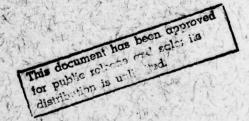
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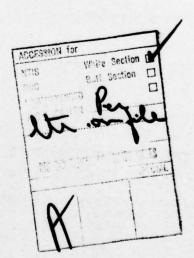
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EOMET '77

Atmospheric Transmission Values Derived from Photographs of the Sea Horizon

1. INTRODUCTION

- 1.1 There is limited experimental evidence that the transmission of the atmosphere at sea during the daytime can be deduced from photographs of the horizon. The experiments which have been reported result in reasonable values of transmission, but no separate measurement of transmission or transmission-related values have been made concurrent with the horizon photographs to demonstrate that the technique is valid.
- 1.2 The 1977 EOMET Cruise presented an opportunity to compare the results of horizon photographs with concurrently measured or recorded meteorological data such as visibility, aerosol concentration and size distribution, nephelometer readings etc. To test the techniques and implement such comparisons, groups of horizon photographs were made on twenty occasions between May 17 and June 6, 1977.
- 1.3 One photograph from each of the twenty groups has been selected by visual inspection to be most promising for data reduction. In addition, a properly exposed but challenging photograph has been selected from ten of the groups. Challenge includes cloud shadows, wind streaks, and white caps.
- 1.4 The horizon photographs were made with color film, and data reduction on a particular film results in three values of atmospheric

scattering coefficient, one in the blue centering on $\lambda_B = 0.44\mu$, one in the green with $\lambda_G = 0.55\mu$ and one in the red at $\lambda_R = 0.64\mu$. The coefficients are appropriate for the sum of molecular and aerosol scattering. Since molecular coefficients are known the aerosol scattering coefficients can be obtained if the method is valid.

The end product of this report is a tabulation of aerosol scattering coefficients at three wavelengths obtained from color photographs of the horizon taken on twenty occasions during the 1977 cruise of the USNS Hayes. In addition, challenging photographs from ten occasions have been analyzed and the scattering coefficients obtained from them are compared with coefficients obtained from the corresponding most promising photographs. Pertinent supporting data are also presented. This includes date, time of day, latitude, longitude, wind direction, ship heading, and cloud type and cover.

2. THEORY

- 2.1 Equations for the apparent radiance of the sea at and near the horizon are developed here. The equations show the relationship between apparent radiance and atmospheric scattering coefficient. In particular, if photographs of the sea horizon are taken from a known altitude above sea level then relative radiance values extracted from the photographs may be used to calculate scattering coefficients.
- 2.2 Figure 1 illustrates the observing conditions. In the figure, ρ is the radius of the earth, R is the distance to the point observed on the sea surface, h is the height of the observer, θ is the depression from the horizontal of the line to the horizon and $\theta + \phi$ is the depression from the horizontal of the point observed. In what follows equations are developed for the apparent radiance of the path from the observer to any point on the sea surface. These equations are so written that if the radiance is measured for various values of ϕ then a value for the scattering coefficient can be obtained. Following this, equations relating R to ϕ are developed. Finally the relationships between positions on the picture of the horizon and values of ϕ are discussed as well as the relationship of exposure of the film at those positions to apparent radiance of the sea surface.
- 2.3 In equation 1 which follows, first order scattering theory is used to describe the apparent radiance $N(\phi)$ of the sea surface at angle ϕ below the line to the horizon.

ow the fine to the horizon.
$$-\int_{0}^{\mathbf{r}} \sigma(\mathbf{r}) d\mathbf{r} - \int_{0}^{\mathbf{R}} \sigma(\mathbf{r}) d\mathbf{r}$$

$$N(\phi) = \int_{0}^{\mathbf{R}} E(\mathbf{r}) \Phi(\mathbf{r}) \sigma(\mathbf{r}) e \qquad d\mathbf{r} + E(\mathbf{r}) g(\mathbf{r}) e \qquad (1)$$

where $N(\phi)$ = the apparent radiance of the sea surface at angle ϕ below the line to the horizon.

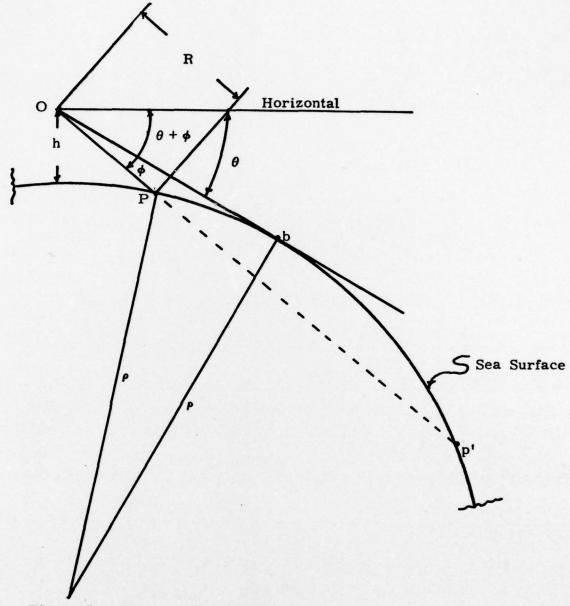


Figure 1. Geometry of the Problem.

Geometry used:

h = height observer's eye in meters

 θ = dip of the horizon in minutes

 $\theta + \phi = \text{dip of point in question in minutes}$

R = distance to point in kilometers

From Bowditch:

R = 2.232
$$(\theta + \phi) - \sqrt{4.982 (\theta + \phi)^2 - 15.35 h}$$

 $\theta = 1.76 \sqrt{h}$

E (r) = total irradiance at position r along path

σ (r) = the effective phase function for scattering from position r toward observing point.

 $\sigma(r)$ = scattering coefficient at r.

g(R) = a coefficient such that g(R) E(R) is the inherent radiance of the sea surface in the direction of the observing point.

2.4 Equation 1 can be solved if three assumptions are made. The first is that the irradiance along the path is constant, the second is that the phase function along the path is constant, and the third is that the inherent radiance of the sea surface is the same for all positions observed. With these assumptions equation 1 may be written

$$N(\phi) = E \Phi[1-e] + E g e$$

$$\int_0^R \sigma(r) dr$$
(2)

The derivative of this radiance as a function of the range to the sea surface, R, is

$$\frac{d}{dR} N(\phi) = E(\Phi - P) \sigma(R) e^{-\int_0^R \sigma(r) dr}$$
(3)

When the data has been taken in the presence of fog there is some range R^* (corresponding to some value of $\phi = \phi^*$) over which the transmission is essentially zero. This implies

$$e^{-\int_0^R \overset{*}{\sigma(r)} dr} \longrightarrow 0 \qquad R \ge R^*$$
 (4)

In clear weather the horizon can be seen so there is no path to the sea surface satisfying equation 4. However, the path just above the horizon is assumed to involve sufficient atmosphere that equation 4 holds. For these two cases, represented by ϕ^* which is positive in fog and negative in clear weather, substitution of equation 4 in equation 2 leads to

$$N(\phi^*) = E\phi \tag{5}$$

2.5 The difference between equation 5 and equation 2 is given in equation 6

$$N(\phi^*) - N(\phi) = E(\Phi - \rho) e^{-\int_0^R o(r)dr}$$
(6)

Finally, equation 3 divided by equation 6 gives the value of the scattering coefficient at distance R. This is shown in equation 7

$$\sigma(R) = \frac{1}{N(\phi^*) - N(\phi)} \frac{d}{dR} N(\phi)$$
 (7)

This may also be written

$$\sigma(R) = -\frac{1}{N(\phi') - N(\phi)} \frac{d}{dr} \left\{ N(\phi^*) - N(\phi) \right\}$$

$$= -\frac{d}{dR} \ln \left\{ N(\phi^*) - N(\phi) \right\}$$

$$= -\frac{d}{dR} \left[\ln \left\{ N(\phi^*) - N(\phi) \right\} - \ln N(\phi^*) \right]$$

$$= -\frac{d}{dR} \ln \left\{ \frac{N(\phi^*) - N(\phi)}{N(\phi^*)} \right\}$$
(8)

This is the key equation for the work discussed here. Further discussion of equation 8 and its application to the data reduction will be made easier by an understanding of the relationship of R to ϕ . Equations showing that relationship are developed next.

- 2.6 Two methods are given here for calculating the distance to a point short of the horizon when the height of the observed is known and the angle of depression of the point relative to the horizon is measured. The first method has its origin in geometrical calculations with no corrections for atmospheric refraction and the second method used empirical relationships which are sensitive to refractive effects and are taken from Bowdich³.
- 2.7 In Figure 1 an observer at 0 views at distance R a point p short of the horizon b. The dip angle of the horizon is θ and the dip angle of the point is $\theta + \phi$. The altitude of the observer is h and the radius of the earth is ρ . Using the cosine law one may write

$$\rho^2$$
 + $(\rho + h)^2 + R^2 - 2(\rho + h) r \cos(\pi/2 - (\theta + \phi))$

or
$$R^2 - 2(\rho + h) r \sin(\theta + \phi) + 2\rho h + h^2 = 0$$
 (9)

Solving for R gives

$$R = (\rho + h) \sin (\theta + \phi) + \sqrt{(\rho + h)^2 \sin^2(\theta + \phi) - 2\rho h - h^2}$$
 (10)

The solution with the positive radical is appropriate to point p in Figure 1. The solution with the negative radical is appropriate for this development as it relates to the point p which is short of the horizon. When the radical is equal to zero the points p and p are coincident and the line of

sight is directed to the horizon. In this case

$$\sqrt{(\rho + h)^2 \sin^2 (\theta + \phi) - 2 \rho h - h^2} = 0$$

or
$$\sin^2\theta = \frac{2\rho h - h^2}{(\rho + h)^2}$$

and
$$\theta = \sin^{-1} \sqrt{\frac{2\rho h - h^2}{(\rho + h)^2}}$$
 (11)

This is the dip of horizon assuming no refraction. Now equation 10 may be written

$$R = (\rho + h) \sin(\theta + \phi) \sqrt{1 - \frac{\sin^2 \theta}{\sin^2 (\theta + \phi)}}$$
(12)

Equations 11 and 12 make up the geometrical solution for the relationship between R and ϕ .

2.8 Bowditch gives an expression for the dip of a point short of the horizon which is rewritten here in metric units as

$$(\theta + \phi) = 0.224R + 3.440 h/R$$
 (13)

where

 $(\theta + \phi)$ is the dip of the point in minutes

h is the height of the observers eye in minutes.

and R is the distance to the point in kilometers.

Solving equation 13 for R, the distance to the point short of the horizon gives

$$R = 2.232 (\theta + \phi) - \sqrt{4.982 (\theta + \phi)^2 - 15.35 h}$$
 (14)

For the case $\phi = 0$ (the line to the horizon)

$$\sqrt{4.982\theta^2 - 15.35 \, h} = 0$$
or
$$\theta - 1.76 \, \sqrt{h}$$
(15)

For the 1977 EOMET work the value of h, the height of the camera lens above the sea surface, was 4.60 meters. Using the geometrical equations gives θ , the depression of the horizon, as 4.13 minutes and the distance to the horizon as 7,656 km. Using Bowditch's equations gives θ as 3.775 min. and the distance to the horizon as 7.810 km. In Figure 2 the range to the horizon calculated using Bowditch's equation, R Bowd' is shown as a function of ϕ . The figure also shows the ratio δ where

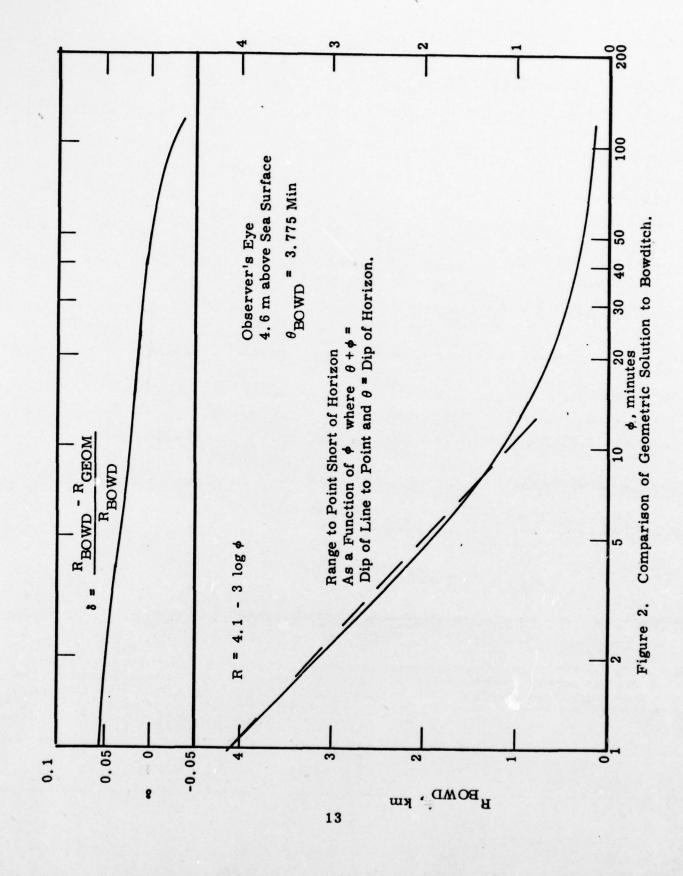
$$\delta = \frac{R_{\text{Bowd}} - R_{\text{Geom}}}{R_{\text{Bowd}}}$$
 (16)

In the data reduction done here Bowditch's equations are used.

Equation 8 relates $\sigma(R)$, the scattering coefficient at range R, to the observable radiances N (ϕ^*) and N (ϕ) where N (ϕ^*) is the radiance just above the horizon or, in fog, at a dip angle ϕ^* small enough so that the specular transmission to the sea surface approaches zero. Equation 8 is repeated here

$$\sigma(R) = -\frac{d}{dR} \ln \left\{ \frac{N(\phi^*) - N(\phi)}{N(\phi^*)} \right\}$$
(8)

Equation 14 is the expression from Bowditch for R, km, the range to a point short of the horizon, when the point has a dip ($\theta + \phi$), min. the



horizon has a dip θ , min and the observer is a height h, m, above the sea surface. As shown in Figure 2, when h = 4.6 m the relationship of R to ϕ in the range $1 \le \phi \le 10$ min can be given by the approximate expressions

$$R = 4.1 + 3 \log \phi {16a}$$

and $\frac{dR}{d\phi} = -\frac{1.3}{\phi} \tag{16b}$

so
$$\frac{1}{R} \frac{dR}{d\phi} = \frac{-1.3}{\phi (4.1 - 3 \log \phi)}$$
 (16c)

- 2.11 In the EOMET experiments h was 4.6 m and the lens of the camera used had a focal length of 50mm. The resolution of the film used was, at best, 50 lines per mm. In a rough way the angular resolution may be taken as $\Delta \alpha = \tan^{-1} \frac{0.02}{50} = 1.38$ min. The probable error in assigning location of the horizon is of the class of \pm one resolution element, or \pm 1.38 min. Table 1 presents calculations using equation 16c of Δ R the uncertainty in range R to points short of the horizon due to $\pm \Delta \alpha$, the uncertainties in the location of the horizon. One film resolution element is taken as the value of $\Delta \alpha$. Values of Δ R are calculated for true distances on the film below the horizon from one to ten resolution elements in length.
- 2.12 In the EOMET experiments there was no effort made to hold the camera exactly horizontal or to point it exactly at the horizon. Location of the horizon image on the films introduces uncertainties in angular position of points short of the horizon of the order of \pm 1.375 min. This uncertainty makes the determination of scattering coefficient as a function of

TABLE 1. ERROR ANALYSIS

Number of film resolution elements from horizon	φ, min	R,km	$\Delta R = \frac{dR}{d\phi} \Delta \alpha$	$\frac{\Delta R}{R}$
0	0	7.810		
1	1.375	3.685	± 1.3	+ 0.35
2	2.750	2.782	± 0.65	± 0.23
3	4.125	2.254	± 0.43	± 0.19
4	5.500	1.879	. ± 0.33	± 0.17
5	6.875	1.588	± 0.26	± 0.16
6	8.250	1.351	± 0.22	± 0.16
7	9.625	1.150	± 0.19	± 0.16

In this table ΔR is the uncertainty in range R to point short of horizon. True point position, ϕ , in minutes, is associated with the number of resolution elements on film below the horizon image. The uncertainty in locating the horizon is $\pm \Delta \alpha$ where $\Delta \alpha$ is taken to be equal to one resolution element which for the lens and film used is 1.375 min.

range, $\sigma(R)$, by use of equation 8 essentially impossible. In a fall-back position it is assumed that the scattering coefficient $\sigma(R) = \sigma$; that is, that the scattering coefficient is independent of range then, from equation 8

$$-\frac{d}{dR} \sigma(R) = 0 = \frac{d^2}{dR^2} \ln \left\{ \frac{N(\phi^*) - N(\phi)}{N(\phi^*)} \right\}$$
 (17)

and

$$-\frac{d}{dR} \ln \left\{ \frac{N(\phi^*) - N(\phi)}{N(\phi^*)} \right\} = const = \sigma$$
 (18)

or a plot of
$$-\ln \left\{ \frac{N(\phi^*) - N(\phi)}{N(\phi^*)} \right\} \text{ vs } R$$

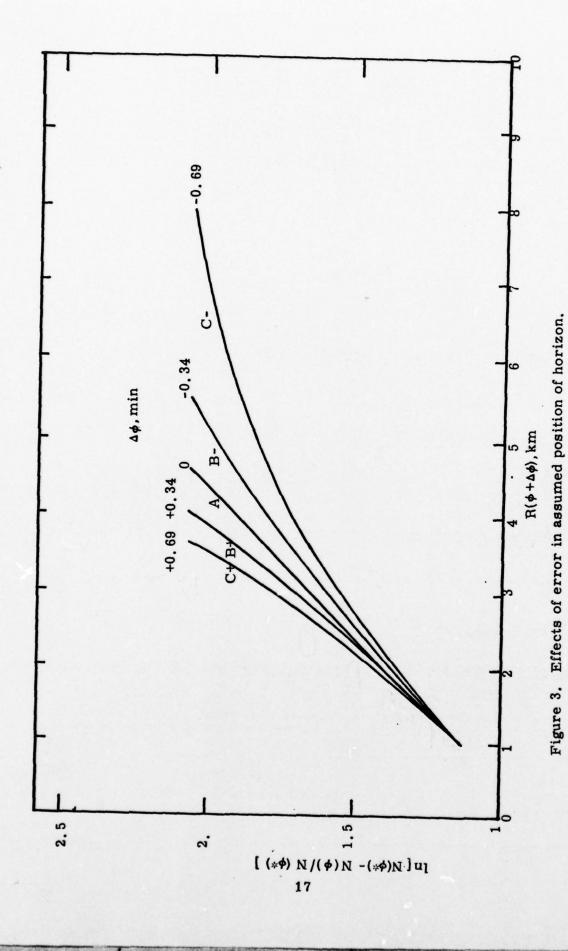
must be a straight line with slope equal to σ

2.13 Figure 3 presents plots of the function

$$f(\phi) = \ln \left\{ \frac{N(\phi^*) - N(\phi)}{N(\phi^*)} \right\}$$
 (19)

VS $R(\phi + \Delta \phi)$

where ϕ is the correct value of the angle between the line to the point in question and the line to the horizon and $\Delta \phi$ is the error in that value. Curve A has no error and is a straight line as required by equation 18. Curves B have errors of \pm 0.34 min (corresponding to 0.25 pixels on film)



and curves C have errors of \pm 0.69 min. In this illustration the range to the horizon is 7.97 km and the correct value of R for point 1 is 4.62 km. There is nothing unique about this. The positive or negative curvature of the plot which results from incorrect guess of horizon image position is characteristic of any case of R < 7.97 km. This feature will be discussed again when the techniques of data reduction are described.

3. DATA REDUCTION

- 3.1 Ektachrome-X film was used for the EOMET horizon photographs. All of the film had the same emulsion number and it was all processed by Eastman Kodak in a single batch along with appropriate sensitometric exposures. Ektachrome-X is a positive color film and by using appropriate optical filters in data reduction the film response in three wavelength bands can be determined. These bands center on wavelengths 0.44μ , 0.55μ , and 0.64μ . A Photometrics Data Systems Microdensitometer was used in data reduction and the first step of the process was to use the sensitometric exposures to establish at each of the three wavelengths the relationship between film density and relative exposure.
- 3.2 Figure 4 is a sketch showing the path on the processed horizon photographs scanned by the microdensitometer. The densitometer slit, which was 1300μ long and 17μ wide was set parallel to the horizon and moved from a position one millimeter above the best guess of horizon image location to a position 5 mm below that location. The density of the film was read automatically every 20μ along the track and these readings were recorded on tape. This process was carried out for each of the three colors, blue, green, and red which were selected by incorporating in the optical train of the densitometer Wratten filters No. 94, No. 93, and No. 92 respectively.
- 3.3 A simple program was set up for a CDC 6600 computer which used the sensitometer data to convert density to relative exposure for each of the three colors. The product of this program is a properly annotated print out of the step number and relative exposure associated with the microdensitometer track across the horizon image. Figure 5 is such a print out and is for frame 13 of the film exposed on 24 May 1977 at 1355. This microdensitometer run was made using a Wratten Filter No. 94, which is blue. The best guess of horizon position was assigned

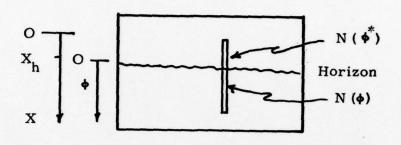


Figure 4. Scanning Track of Photographs

		FILM SEGME	NT FRAME	DATE 24 MAY 7	1 1 ME 1 355	1DEN P3508HPS01	SOLOR SLUE = 94			TW
X (HH)	PEL	X X	REL	X (HH)	REL	X (HH)	REL	(H4)	REL EXP	
9.00	11.16	9.02	11.16		11.16		11.33	9.08	11.00	
9.20	11.16	9.12	11.15	9.14	11.16	9.16	11.16	9.18	11.00	
9.50	11.00	9.32	11.00	9.34	10.64	9.36	10.84	9.30	10.84	
9.48	10.84	9.42	10.84	9.44	10.84	9.46	11.00	9.48	11.00	
9.00	17.84	9.62	10.84	9.64	11.00	9.56	10.84	9.58	10.84	
9.70	10.64	9.72	14.84	9.74	11.00	9.76	10.84	1.76	11.00	10,89
9.96	10.84	9.8?	11.00	9.84	10.84	9.86	11.00	9.88	10.84	
0.03	10.68	10.02	10.37	10.04	8.68	10.06	7.53	10.08	7.15	
0.10	6.19	10.12	6.75	10.14	6.61	10.16	6.61	10.18	6.35	
J. 30	5.95	1 32	6.03	10.34	5.95	10.36	5.95	10.38	5.87	
0.40	5.7?	10.42	5.00	10.44	5.80	10.46	5.95	10.48	5.87	
0.50	5.72	10.52	5.65	10.54	5.65	10.56	5.57	10.58	5.57	
0.76	5.40	10.72	5.35	10.74	5.40	10.76	5.35	10.76	5.45	
06.0	5.35	10.62	5.35	10.84	5.30	10.86	5.21	10.88	5.35	
1.00	5.40	11.02	5.35	11.04	5.35	11.06	5.30	11.08	5.21	
1.10	5.25	11.12	5.35	11.14	5.21	11.16	5.16	11.18	5.30	
1.30	5.11	11.22	5.16	11.34	5.48	11.26	5.35	11.28	5.21	
1.40	5.45	11.42	-5.45	11.44	5.40	11.46	5.30	11.48	5.16	
1.50	5.21	11.52	5.15	11.54	4.97	11.56	4.97	11.58	5.16	
1.76	5.25	11.62	5.40	11.74	5.35	11.66	5.50	11.68	5.21	
1.00	4.84	11.82	4.84	11.84	4.75	11.86	5.02	11.68	5.21	
1.46	5.45	11.92	5.35	11.94	5.65	11.96	5.45	11.98	5.40	
2.10	5.50	12.12	5.35	12.14	5.02	12.16	4.84	12.16	4.62	
2.28	4.54	12.22	4.05	12.24	5.11	12.26	5.16	12.28	5.30	
2.30	5.16	12.32	4.84	12.34	4.75	12.36	4.80	12.38	4.88	
2.50	4.93	12.52	4.97	12.54	4.93	17.56	4.62	12.58	4.58	
2.60	5.07	12.62	4.38	12.64	5.40	12.66	5.35	12.66	4.67	
2.80	5. 35	12.62	5.25	12.84	5.02	12.86	4.50	12.88	5.16	
2.90	4.50	12.92	4.88	12.94	4.93	12.96	4.80	12.98	5.11	
3.10	5.45	13.02	5.35	13.04	5.16	13.06	5.02	13.00	5.07	
3.20	5.25	13.22	5.30	13.24	5.07	13.26	5.07	13.28	5.07	
3.40	5.02 4.93	13.32	4.97	13.34	5.02	13.36	4.80	13.38	5.07	
3.50	5.07	13.52	5.11	13.54	5.16	13.56	5.21	13.56	5.25	
3.60	5.16	13.62	5.11	13.64	4.97	13.66	5.07	13.68	5.11	
3.70	5.07	13.72	5.15	13.74	5.21	13.76	4.34	13.76	4.50	
3.90	4.54	13.92	4.85	13,94	5.11	13.96	5.11	13.98	5.25	
4.00	5.21	14.02	5.07	14.14	4.84	14.06	4.38	14.08	4.75	• • • • • • • • • • • • • • • • • • • •
4.20	4.93	14.22	5.02	14.24	5.25	14.26	5.25	14.28	4.88	
4.30	4.71	14.32	4.39	14.34	4.38	14.36	4.67	14.38	4.97	
4.51	5.11	14.42	4.71	14.44	5.02	14.46	5.62	14.58	5.21	
4.60	5.07	14.62	4.93	14.64	4.88	14.66	4.71	14.68	4.67	
4.70	4.58	14.72	4.42	14.74	4.22	14.76	4.67	14.78	4.54	
4.90	4.66	14.92	5.07	14.94	4.88	14.86	4.84	14.98	4.75	

Figure 5. Values of relative exposure from horizon trace.

track distance scale value of 10.00 mm. The trace was started above the horizon image at 9.00 mm and run to 15.00 mm.

- 3.4 The relative exposure values for the 15 points between 9.60 mm and 10.84 mm were averaged (10.89) and used as N (ϕ *) the relative radiance of the sky above the horizon. The exposures in the sequence starting at 9.98 were scanned visually and sequential differences noted. The exposure (8.68 at 10.04) following the greatest sequential difference (10.37-8.68) was selected as the first of a series of nine values of N (ϕ) to be used in calculating the scattering coefficient.
- 3.5 A program for an HP-97 was used to calculate

$$f(x - x_0) = -\ln \left\{ \frac{N(\phi^*) - N(\phi)}{N(\phi^*)} \right\}$$
 (20)

for each of the nine values of N (ϕ) and also the ranges, R, for each of the nine values of (x-x_o) in the microdensitometer track assuming some position x_o for the horizon. The HP-97 program calculated the linear regression corresponding to

$$f(x-x_0) = A + BR(x-x_0)$$
 (21)

for the first five values of (x-x), yielding B_5 and then for the nine values of (x-x), yielding B_9 . The ratio B_5/B_9 was calculated and if this was within one percent of unity the selected position for the horizon was accepted otherwise a new position for the horizon (x) was chosen. Usually no more than four such iterations of this sort were necessary. The final value of B_9 , the slope of the regression, was taken as σ , the scattering coefficient. The program then could print out the nine pairs of values N (ϕ) and R appropriate to the nine values of (x-x). The following values

from Figure 4 were used in this process:

N	(φ [*])		=	10.89		
N	(ϕ) ,	1	=	8.68	at	10.04
		2	=	7.53		10.06
		3	=	7.15		10.08
		4	=	6.78		10.10
		5	=	6.78		10.12
		6	=	6.61		10.14
		7	=	6. 61		10.16
		8	=	6.35		10.18
		9	=	6.19		10.20

In the iteration to find the horizon position the following values of x were used resulting in the associated values of B_5/B_9 .

B ₅ /B ₉
1.18
0.975
1.06
1.02
1.008

Using the value $x_0 = 10.0395$ values of $f(x-x_0)$ and R are

R,km	f(x-x ₀)
7.18	1.59
3.62	1.18
2.65	1.07
2.12	0.974
1.77	0.974
1.53	0.934
1.35	0.934
1.20	0.850
1.09	0.840

The regression is given by

$$f(x-x_0) = 0.744 + 0.119 R (x-x_0)$$
 (22)

hence $\sigma = 0.119 \approx 0.12 \text{ km}^{-1}$.

3.6 In this work 30 films have been analyzed in three colors leading to 90 possible values of σ . Of these 53 have been done as described above, 12 have been done using nine averages of sequential groups of five (45 values of N (ϕ) in total), 3 have been done with sequential groups of fifteen and one with sequential groups of 3. Of the remaining 21, 18 have been done by hand and involved less than five groups of from 1 to 15 values of N (ϕ) per group and three defied analysis. Values of σ so obtained are presented in Table 2.

TABLE 2. Values of Scattering Coefficient, km⁻¹

Date	e	Time	Dem	onstratio	n	Cha	allenge	
			0.44μ	0.55μ	0.64μ	0.44μ	0.55μ	0.64μ
May	17	1320	2.42	1.95	1.63 (5,9)			
	18	0945	28	8.5	3.5 (15,6)	3.48	3.17	2.79 (15,9)
	18	1700	0.12	0.11	0.10 (1,9)	0.20	0.15	0.08 (1,9)
	21	1545	0.21	0.17	0.10 (1,9)	0.36	0.24	0.28(1,5)
	22	1230	0.19	0.22	0,20 (1,9)	0.62	0.52	0.51 (1,5)
	22	1830	0.08	0.06	0.08 (1,9)	0.23	0.29	0.29 (1,9)
	23	1100	0.16	0.13	0.12 (1,9)			
	24	1030	0.25	0.18	0.19 (1,9)			
	24	1355	0.12	0.08	0.06 (1,9)	1.45	1.25	1.29 (5,9)
	25	1055	0.17	0.19	0 17 (1,9)	÷		
	25	1610	0.13	0.085	0.086(1,9)			
	26	0925	0,27	0.33	0.21 (1,9)	0.51	0,42	0.45(1,5)
	26	1530	0.43	0.31	0.25 (1,9)	0.41	0.36	0.47(1,4)
	27	0950	4.09	2.97	1.99 (5,9)			
	31	1050	0.37	0.29	0.19 (1,9)	I	ailure	
June	1	1240	0.16	0.14	0.12 (1,9)			
	3	1230	0.16	0.15	0.19 (1,9)			
	4	1505	0.56	0.45	0.35 (1,9)			
	5	1440	0.67	0.53	0.38 (1,9)	1.61	0.92	1.08 (5,4)
	6	1330	0.92	0.91	0,85 (5,9)			

DEMONSTRATION VALUES ARE FROM FRAME SELECTED VISUALLY AS EASIEST TO REDUCE.

CHALLENGE VALUES ARE FROM FRAMES SELECTED VISUALLY TO BE PROPERLY EXPOSED BUT DIFFICULT TO REDUCE.

UNDERLINED VALUES OBTAINED BY SPECIAL HAND PROCESSING.

OTHER VALUES OBTAINED BY SEMI-HANDS-OFF METHOD.

VALUES IN PARENTHESES (1,9), (15,6) etc REPRESENT NUMBER OF SEQUENTIAL VALUES OF N (\$\phi\$) AVERAGED IN A GROUP FOLLOWED BY NUMBER OF GROUPS INVOLVED IN A PLOT. 3.7 Each value of σ quoted in Table 2 represents the slope of an associated plot of values of $f(x-x_0)$ vs $R(x-x_0)$. All such plots are presented in Appendix A. The processed data from each horizon photograph analyzed (with the exception of the one failure) is presented in the appendix as three plots drawn on one page. These are the plots of

$$\ln \left\{ \frac{N(\phi^*) - N(\phi)}{N(\phi^*)} \right\} = f(x - x_0) \text{ vs } R(x - x_0).$$

The plots are for the blue, the green and the red image of the horizon. The plots are identified by date and Greenwich mean time. The letter D in the upper right hand corner identifies a demonstration run and the letter C a challenge. The values of total scattering coefficient, which is the slope of the plots shown, are given for the three colors as are the associated aerosol scattering coefficients. Certain meteorological information with the plots and other supporting information is given in Table 3.

TABLE 3. PHYSICAL AND METEOROLOGICAL CONDITIONS

% Cloud Cover		20 Ac Trans	Fog-xx	<1 Ci Fibr.	100 xx	40 Cu Fair Weather	90 Cu Fair Weather, Ci Fibr.	50 Sc Cumulog, Ac Trans undul,		100 xx	60 Ac Trans overhead downto 300	100 St cover Rainclouds 3000 ft.	100 Cu Fair Weather, Cs	1 Cs	20 Fair Weather St, Sc Cumulog	80 St Fract, Fair Weather Cu	100 Ac Trans, As Opacus	40 Ci Fibr, Ac Trans, Cu Fair	5 Fair Weather Cu	50 Fair Weather Cu, Congestus	5 Fair Weather Cumulus
Ship Head. True	deg.	043	090	061	660	274	160	105	100	100	114	113	231	115	021	075	058	145	145	320	046
True Wind Direct.	deg.	229	318	136	318	300	290	020	178	175	187	198	205	274	348	304	251	330	311	306	310
Longitude	. min.	32,402	4.712	32.8	2.0	4.4	58.45	37.7	30.027	37.0	23.0	14.8	29.95	50.8	29.45	27.9	47.9	23.2	26.0	19.0	56.2
Lon	deg.	65	62	09	42	37	36	31	25	24	19	18	14	13	6	က	-	-12	-15	-,19	-22
Latitude	min.	42 37.889	37.043	9.000	50.1	16.1	5.1	30.7	6, 159	58.4	34.6	8.1	35.25	30.7	0.9	39.0	52.9	48.0	39.1	7.1	20.7
Lat	deg	42	44	45	44	44	44	43	43	41	40	40	38	38	37	35	37	36	33	33	35
GMT	1	1320	0945	1700	1545	1230	1830	1100	1030	1355	1055	1610	0925	1550	0980	1050	1240	1230	1505	1440	1330
DAY		17	18	18	21	22	22	23	24	24	25	25	92	26	27	31	1	8	4	ß	9
MONTH		May															June				

4. DISCUSSION

- the horizon was photographed give reasonable values for the total scattering coefficient in the blue the green and the red. These values have been obtained by an almost automatic process of data reduction. Operator involvement occurs in the selection of the best guess position of the horizon and the changes of this guessed position in the iteration process. The twentieth occasion, May 18 at 0945, required hand reduction of the data and yielded unreasonable results. It should be noted that the challenge picture selected for this occasion yielded rather reasonable values of the scattering coefficients.
- The photographs selected as challenges seem to produce 4.2 reasonable values of the scattering coefficients; however, there is only rather general agreement between simultaneous challenge and the demonstration values. The values on May 24 at 1355 are different by more than an order of magnitude. In this case the demonstration, data reduction was carried out the "automatic" process and involved the use of nine adjacent pixels for data processing. In this case the values of scattering coefficient have been determined by optical effects occuring within the range between approximately 1 and 4.6 km from the ship. The corresponding challenge data were also reduced "automatically" however, using the first nine pixels below the horizon did not work well in the "automatic" process so nine sequential groups of 5 pixels per group were used. In this case the values of scattering coefficient have been determined by optical effects occuring within the approximate range 0.25 to 2.4 km. Inspection of the picture used for the challenge shows a dark streak on the sea extending from about 0.16 km from the ship to roughly 1.3 km. This may account for the results obtained with this film.
- 4.3 As noted before, the challenge picture for 31 May at 1050 could not be analyzed either "automatically" or by hand.

5. CONCLUSIONS

The following conclusions seem justified:

- 1. Color photographs of the sea horizon can be used to determine scattering coefficients at λ = 0.44 μ , λ = 0.55 μ , λ = 0.64 μ .
- 2. The semi-hands-off calculations demonstrate that completely automatic data analysis is feasible.
- 3. Such an analysis system could be used in a real time system involving, for instance, scanning or a silicon diode array.
- The existing films could be used as a data bank for simulations of the behavior of proposed real time systems.

REFERENCES

- 1. H. S. Stewart and A. H. Pierson, J. Opt Soc Am. 64, 550A (1974).
- 2. Kabanov, M. V. and Sakerin, S. M., "Determination of the Extinction Coefficients for Optical Radiation in the Atmosphere from the Softening of the Horizon Line", Isvestiya, Atmospheric and Ocean Physics, Vol 13, No. 5, 1977.
- 3. Bowditch, N., "American Practical Navigator", H.O. Pub. No. 9, U.S. Navy Hydrographic Office, 1958.

APPENDIX A

Processed Data

In the following pages three graphs are presented for each film analyzed. Each page is specific to a particular film identified by date and time. In addition the letter D or C identifies demonstration pictures or challenge pictures.

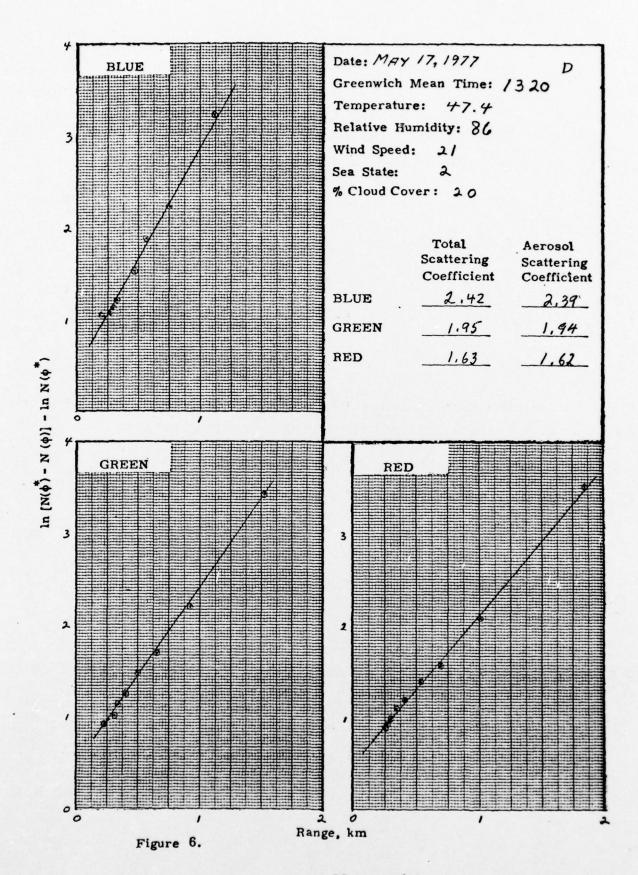
The graphs are of the function

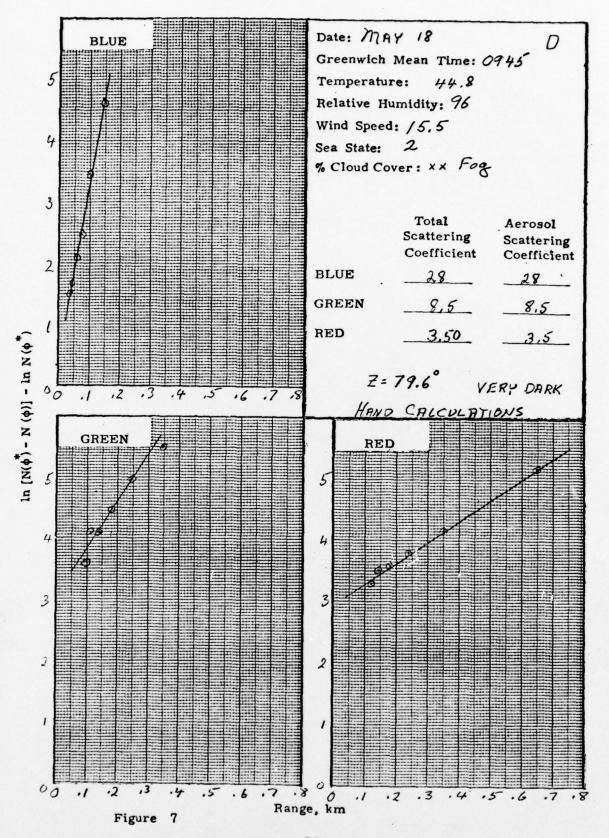
$$\ln \left\{ \frac{N(\phi^*) - N(\phi)}{N(\phi^*)} \right\}$$

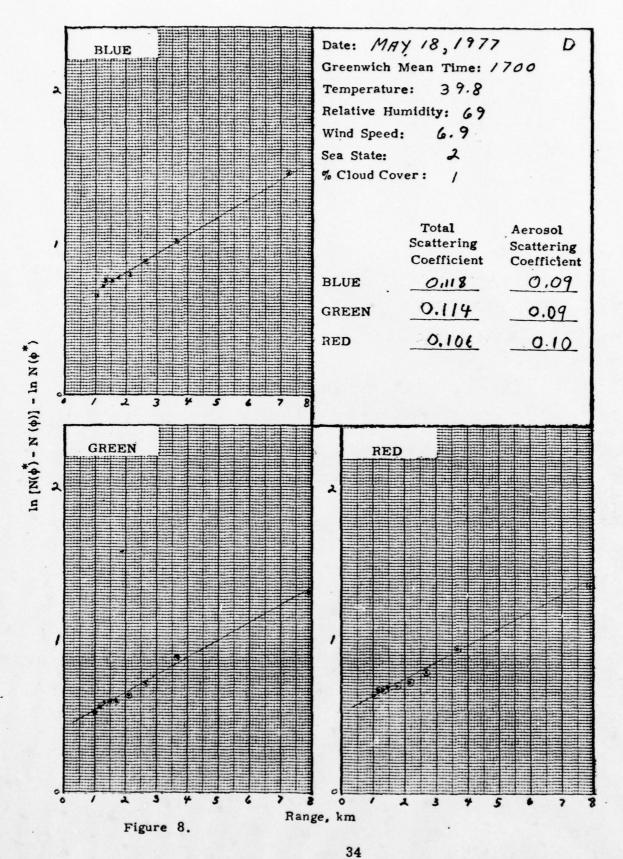
vs $R(\phi)$. It has been shown that if the graph is a straight line the locus of the horizon (ϕ = o) has been selected correctly and the slope of the straight line is equal to the scattering coefficient.

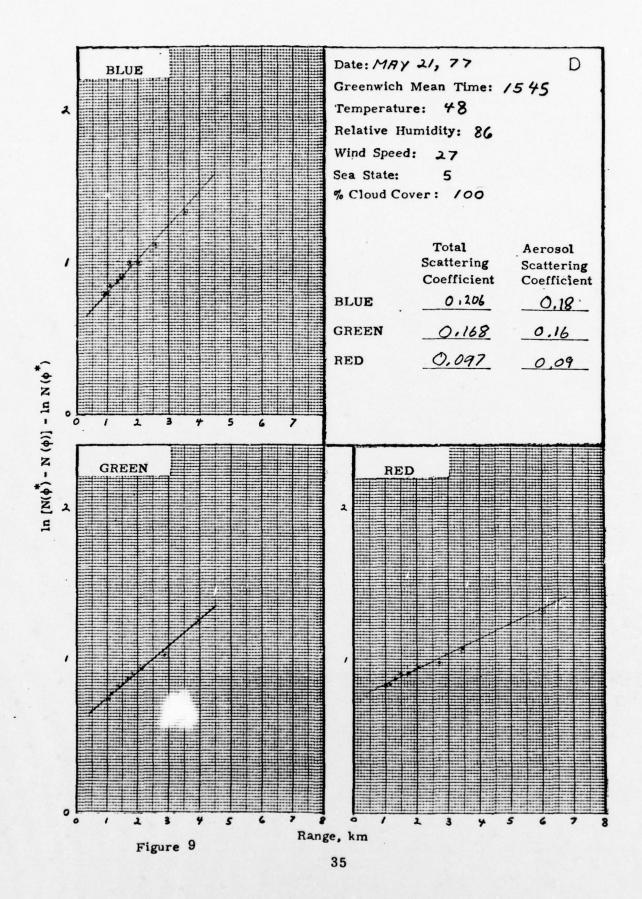
Twenty pages of graphs representing the reduced data for the demonstration films are presented in sequence of times the pictures were taken.

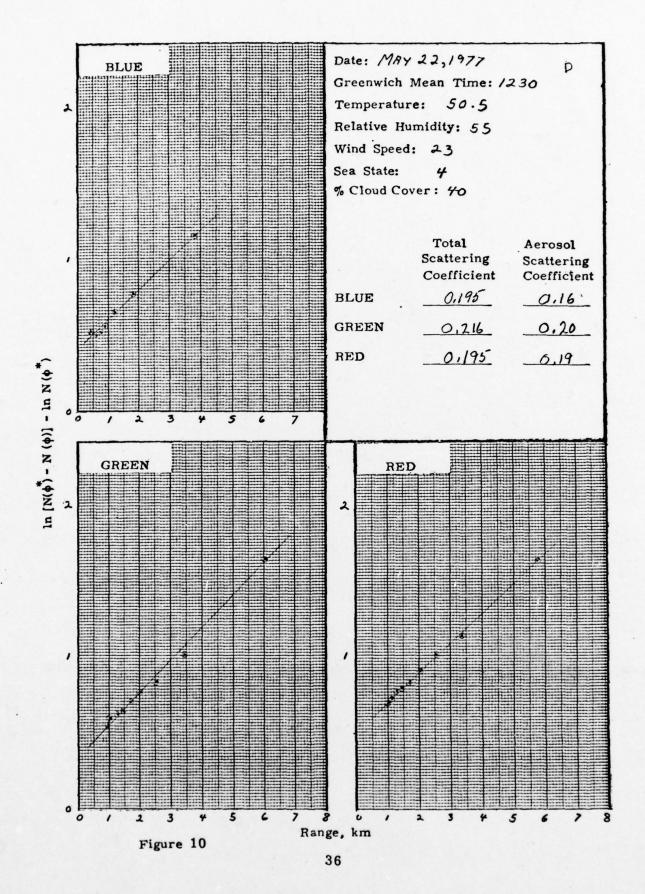
Following this nine pages of challenge graph are given. Interspersed are five black and white enlargements of the color pictures used. The demonstration picture included is for 3 June at 1230. Challenge pictures are 18 May at 0945, 21 May at 1545, 22 May at 1230 and 22 May at 1830. Finally a print of the densitometer trace across the horizon is given for the blue image on the challenge film for 21 May at 1545.

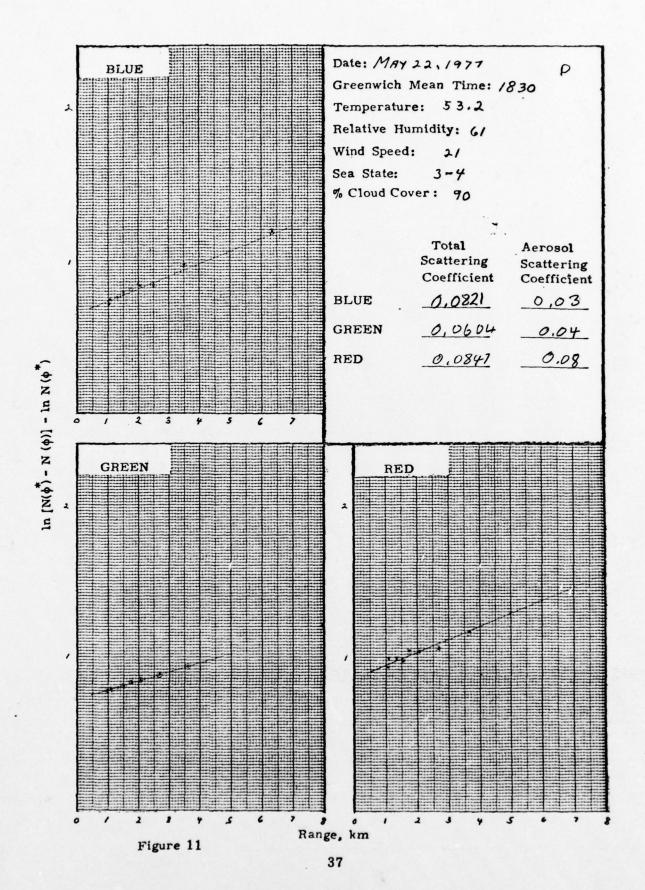


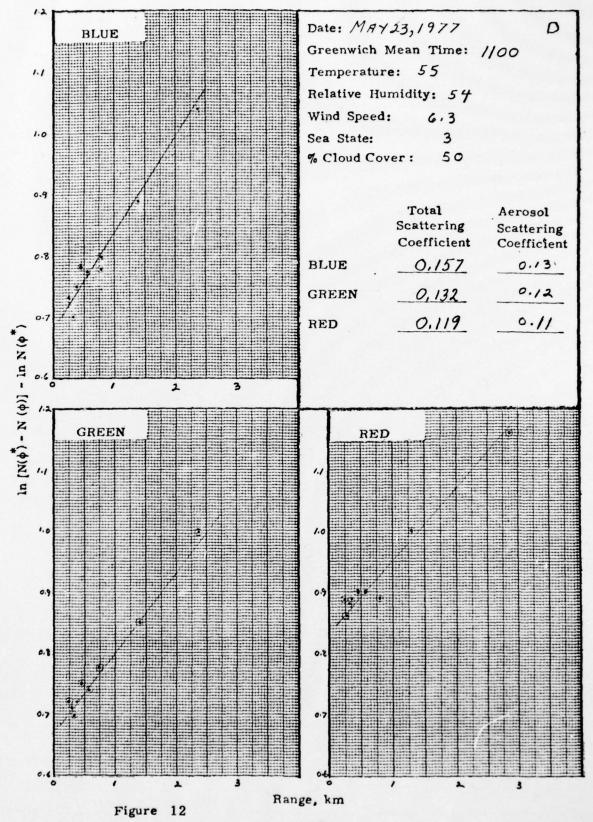




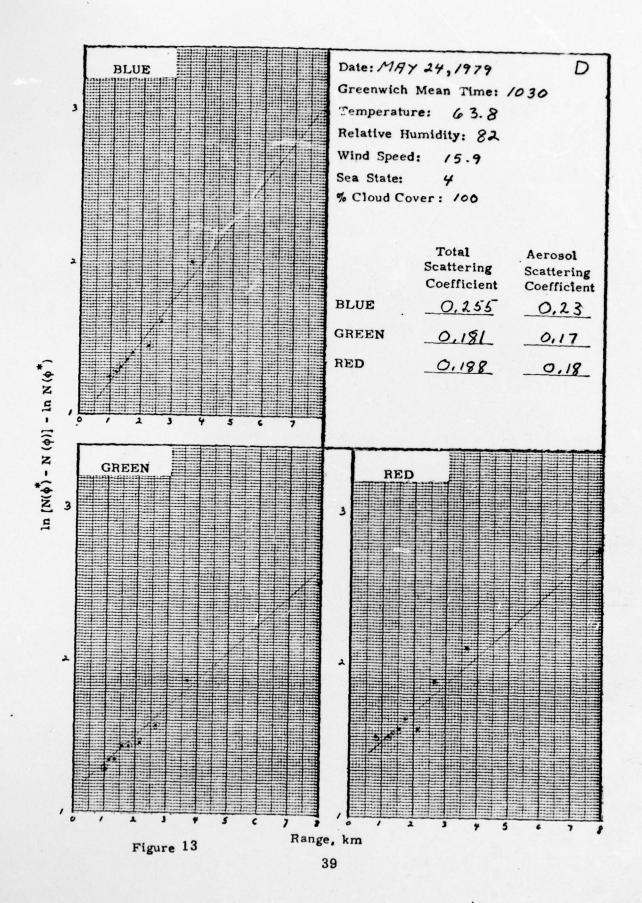


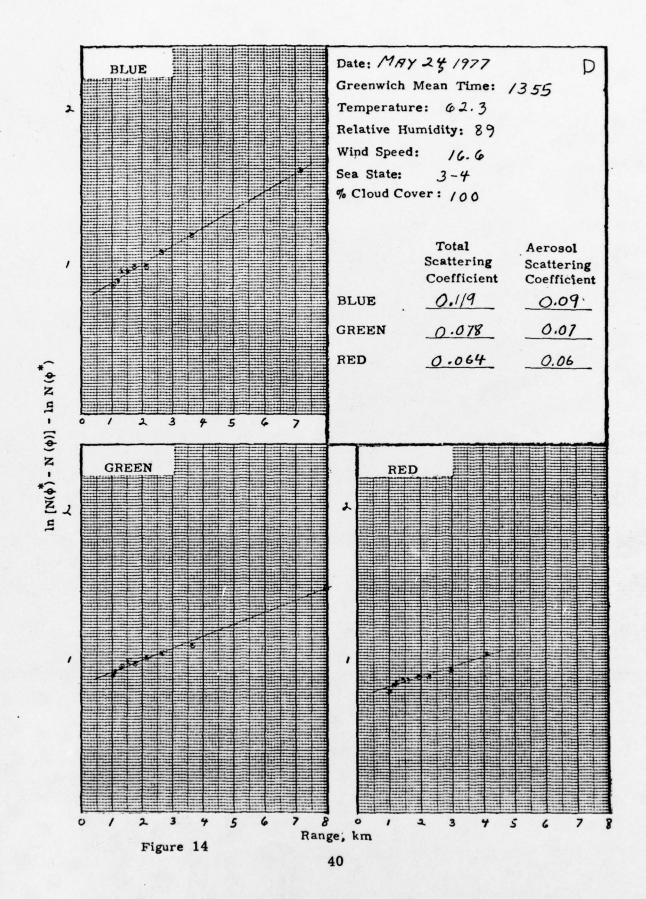


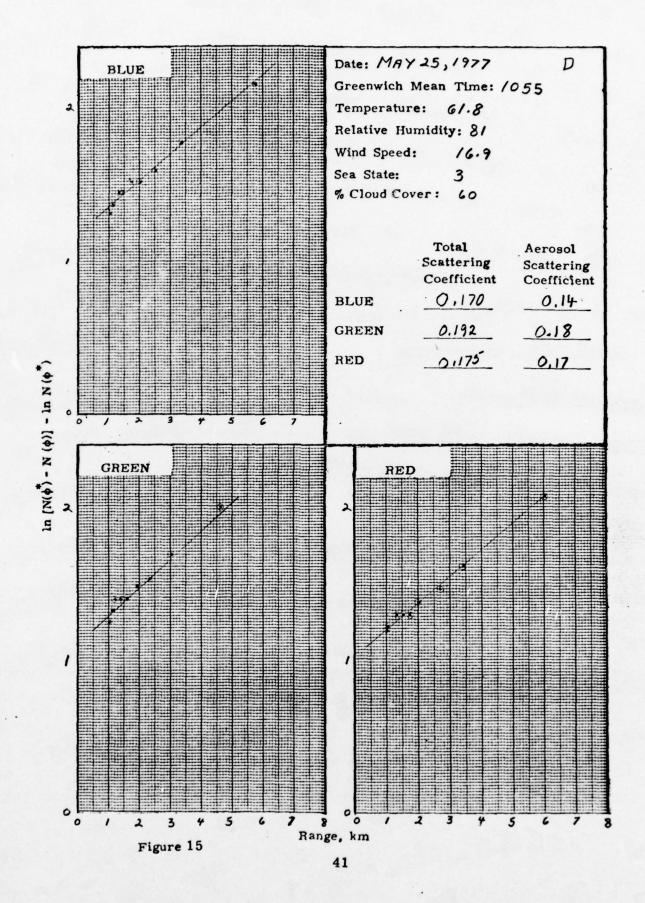


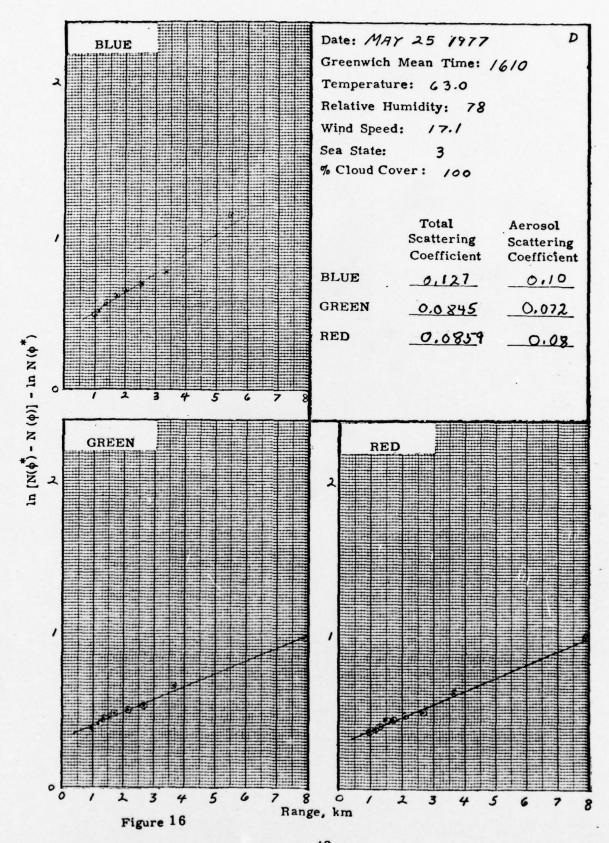


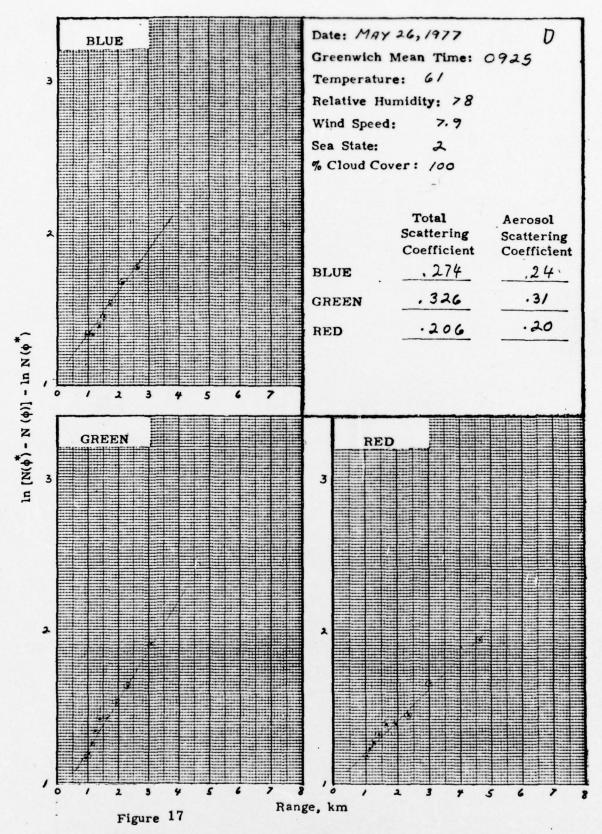
NOT LESS TO

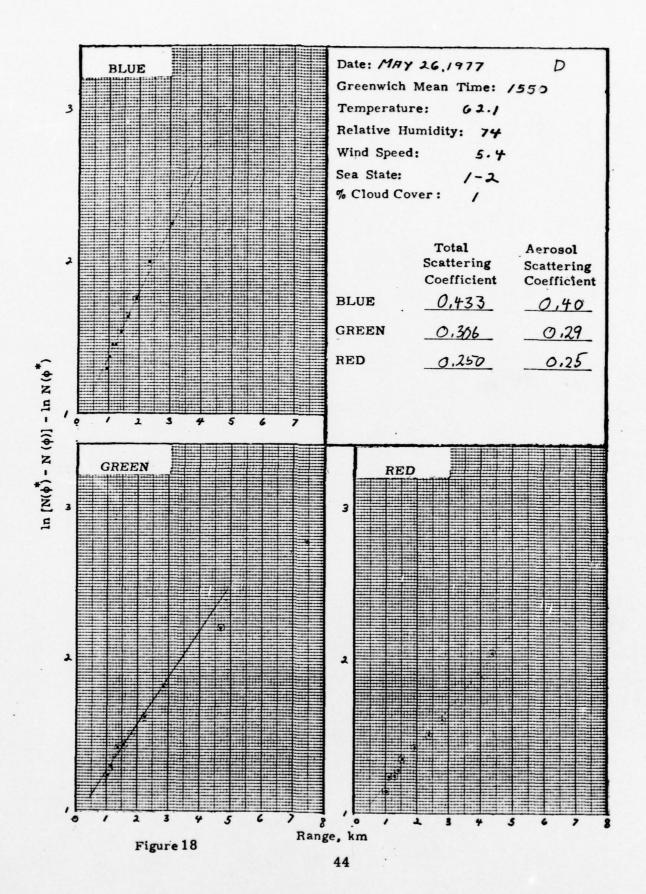


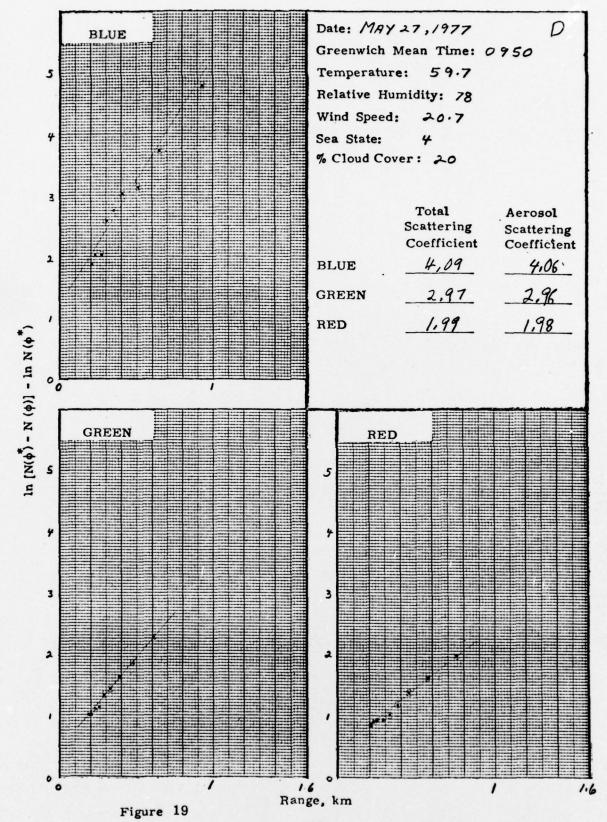


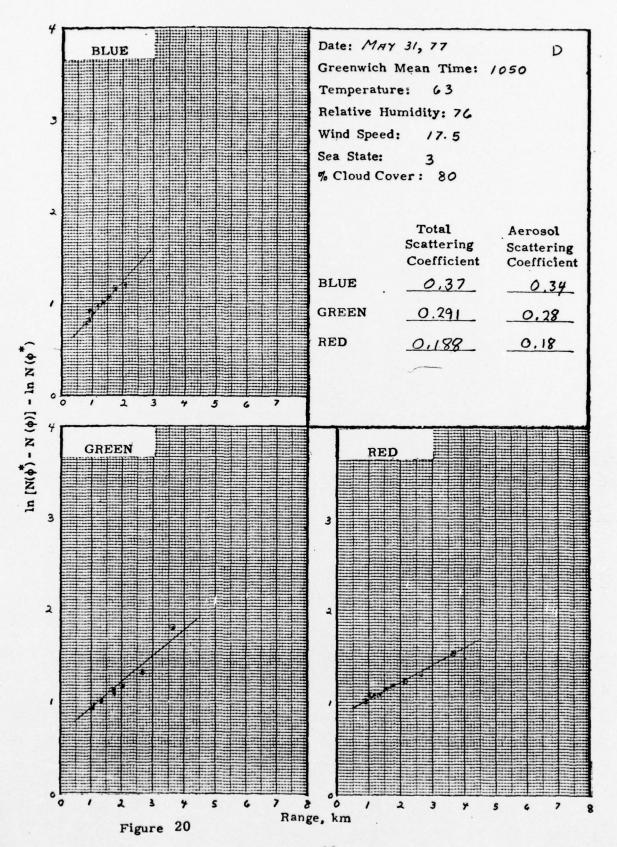


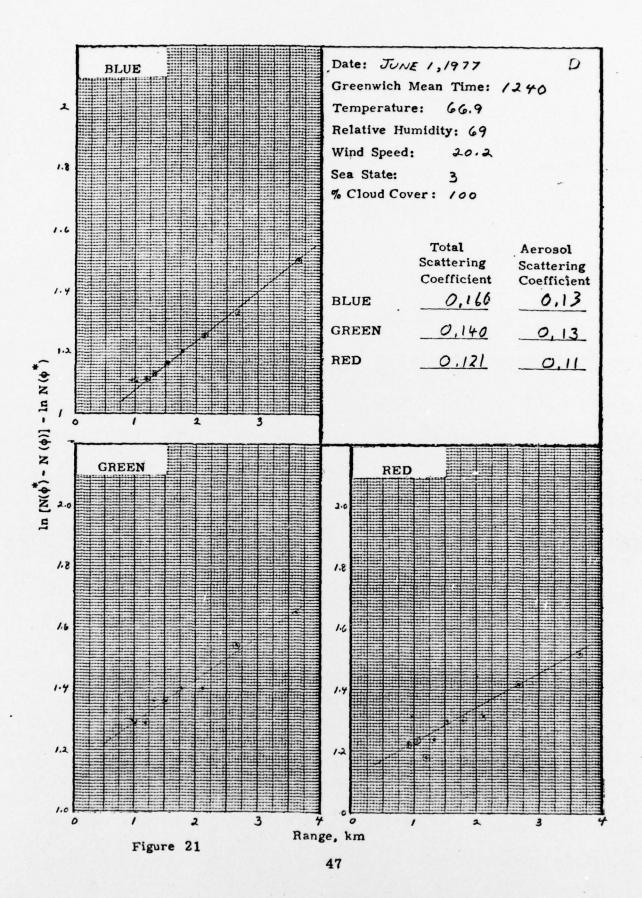


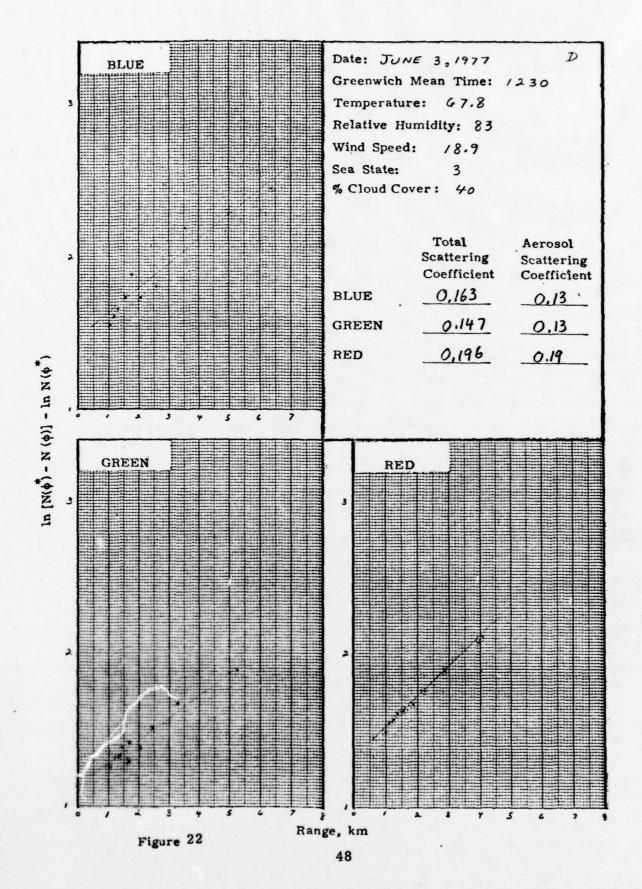












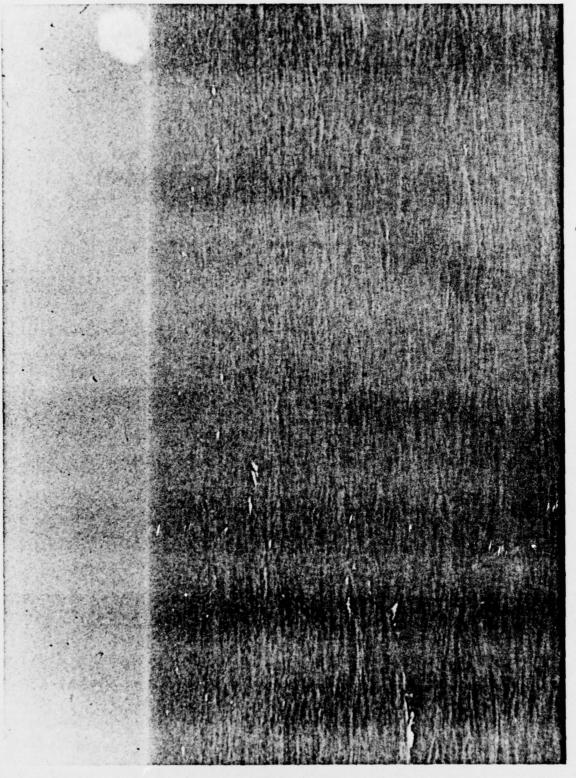
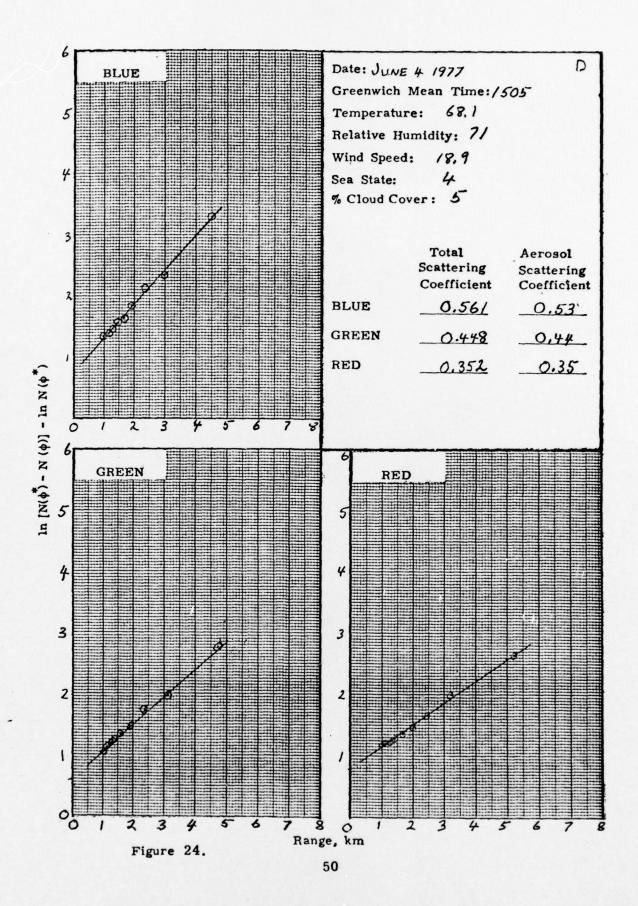
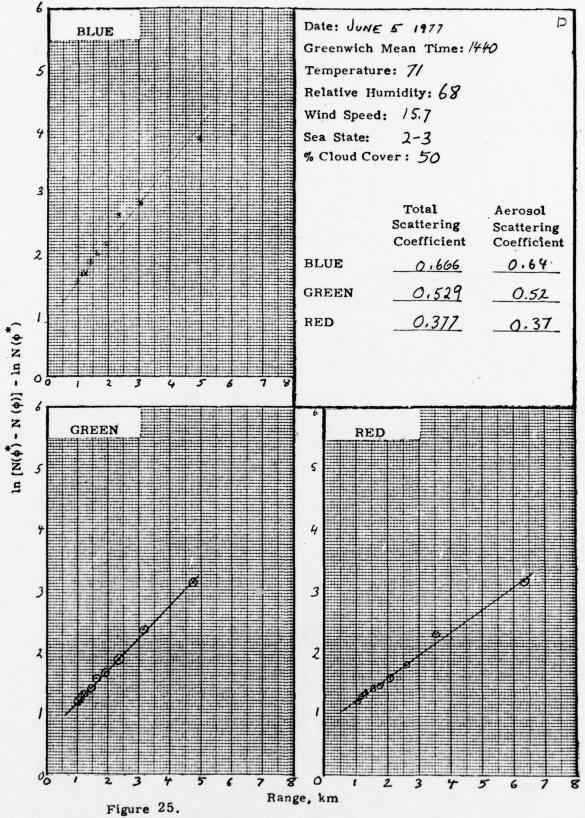
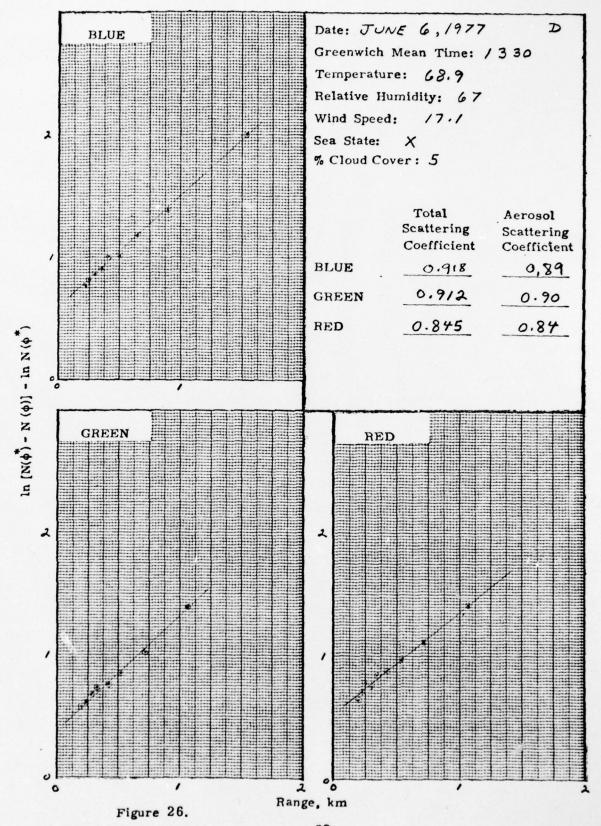


Figure 23. June 3,1977 Time 1230, EOMET Film 16 FR16 Segment 3.







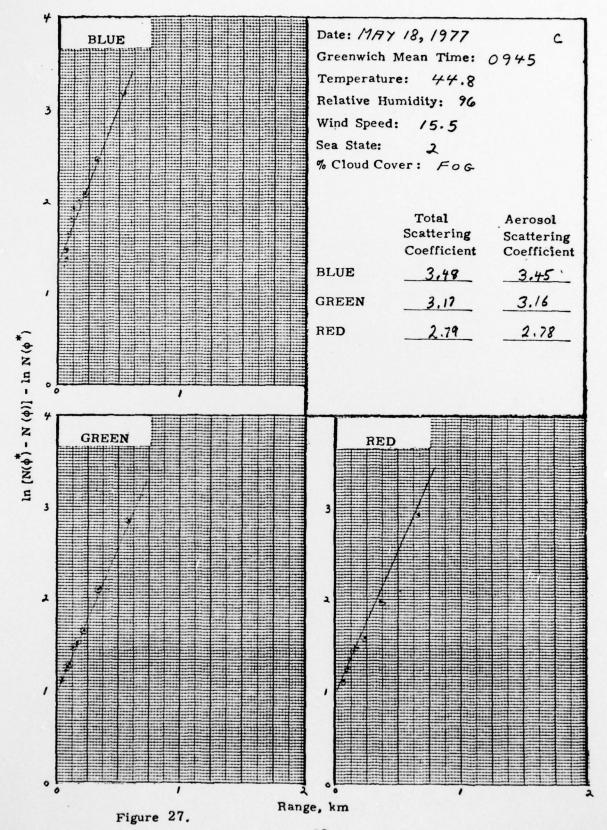
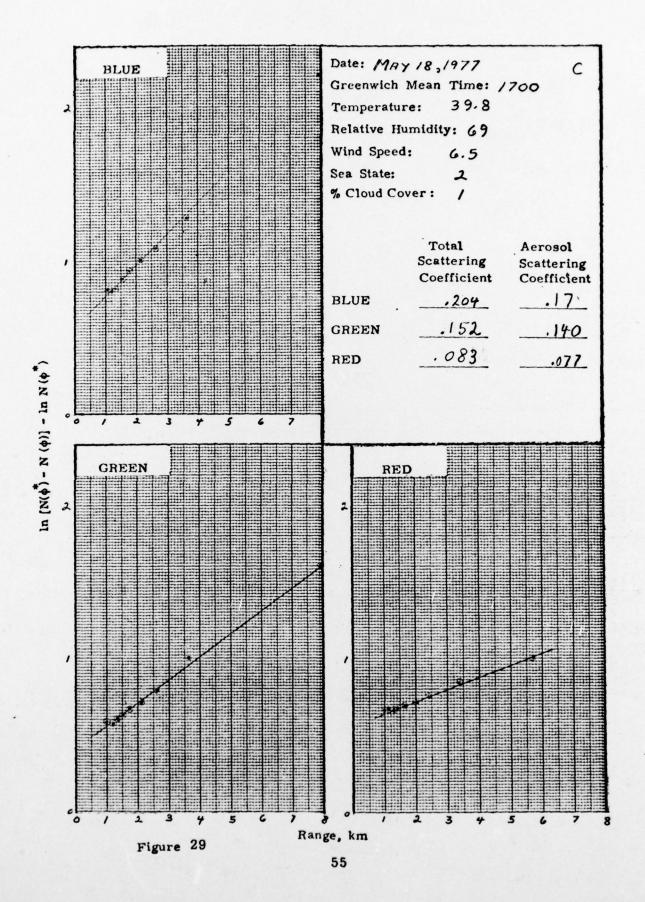
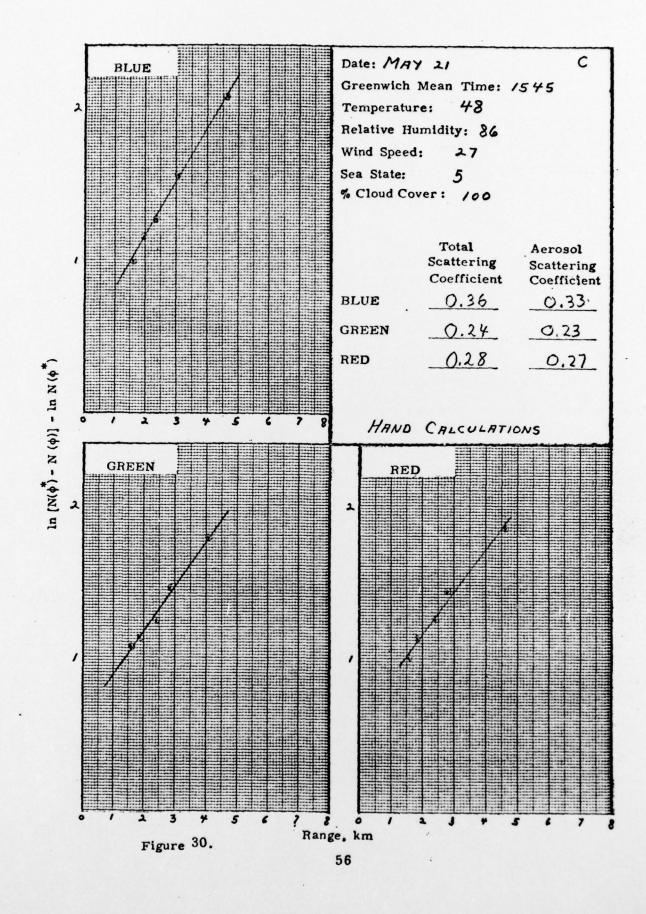


Figure 28. May 18, 1977 Time 0945. EOMET FR15 Film 2 Segment 3.





igure 31. May 21,1977 Time 1545 EOMET Film 4 FR11 Segment 2.

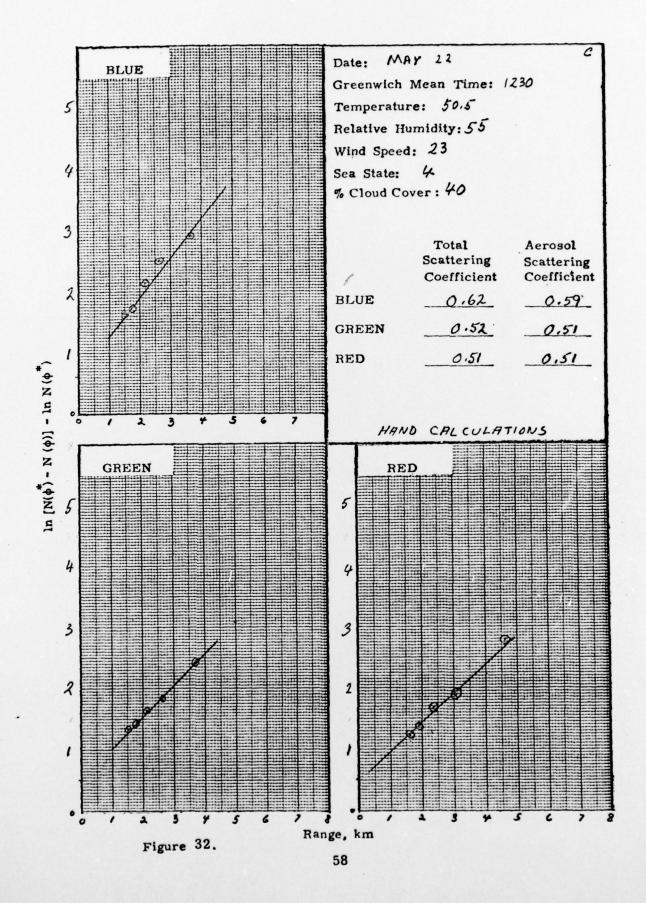
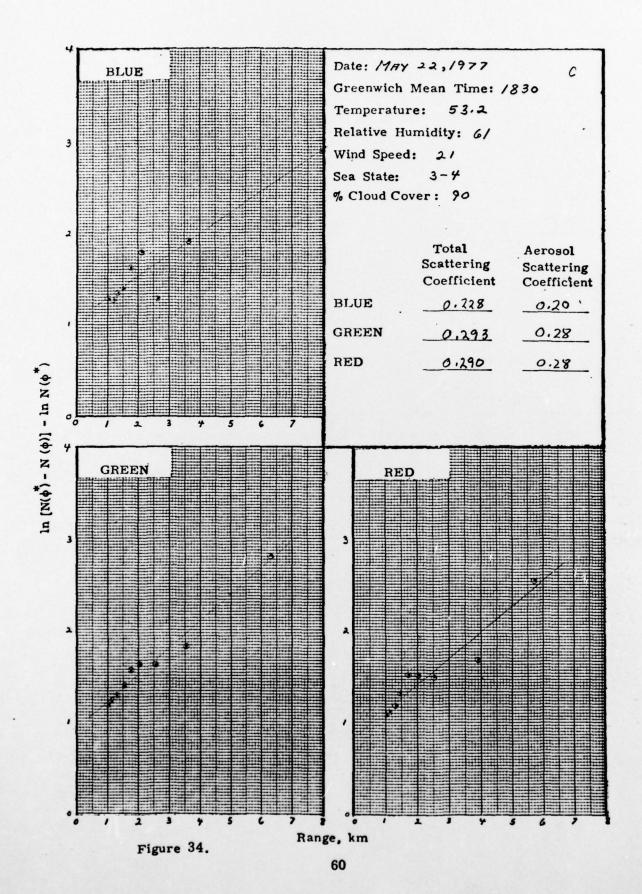




Figure 33. May 22, 1977 Time 1230 EOMET FR9 Film 5 Segment 2.



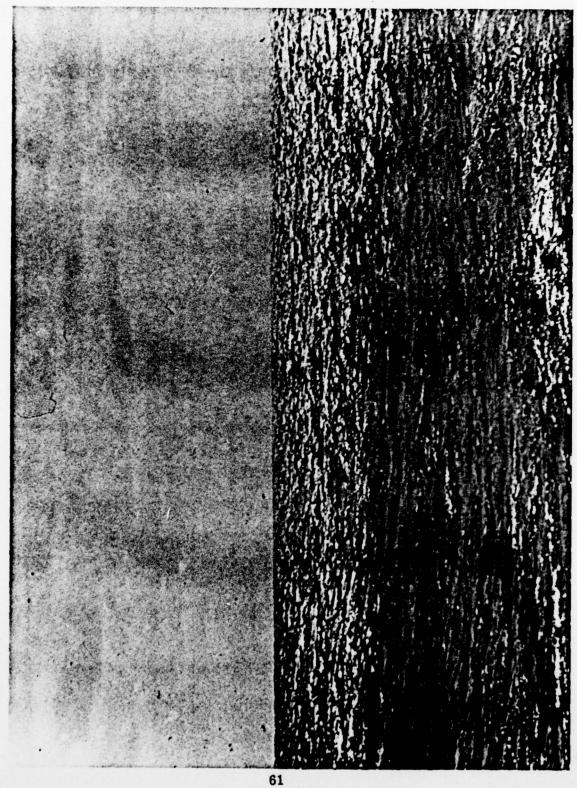
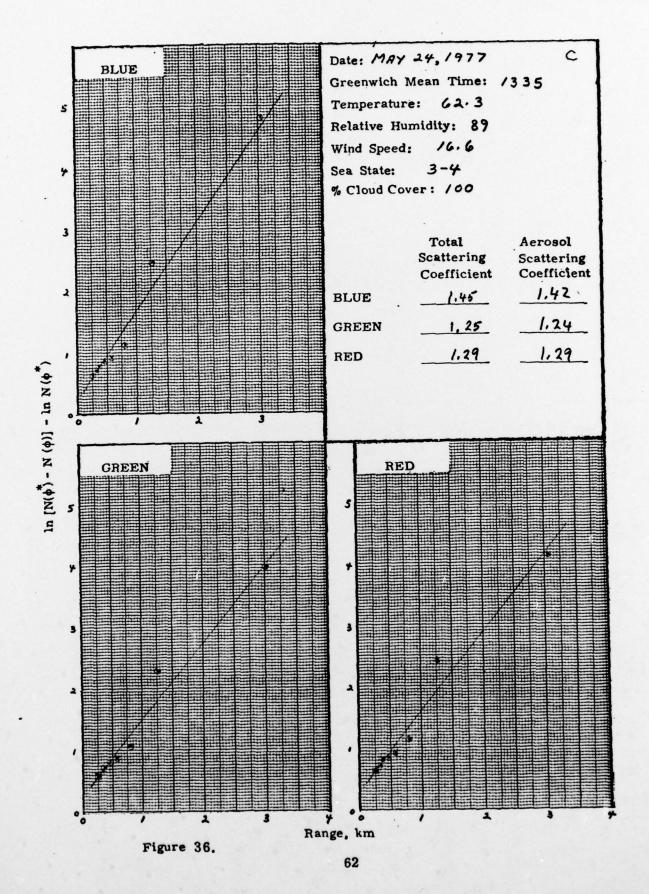
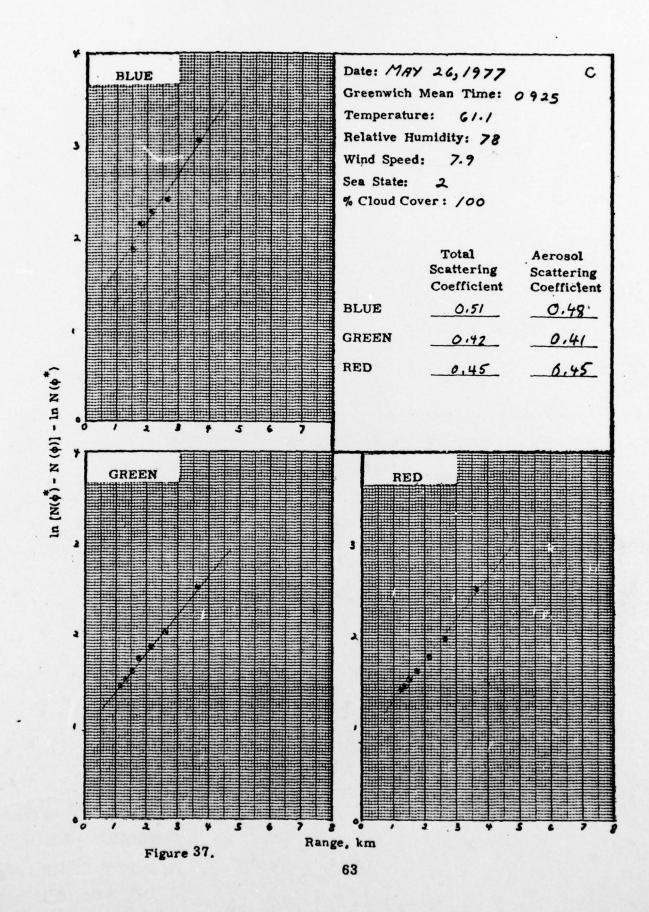
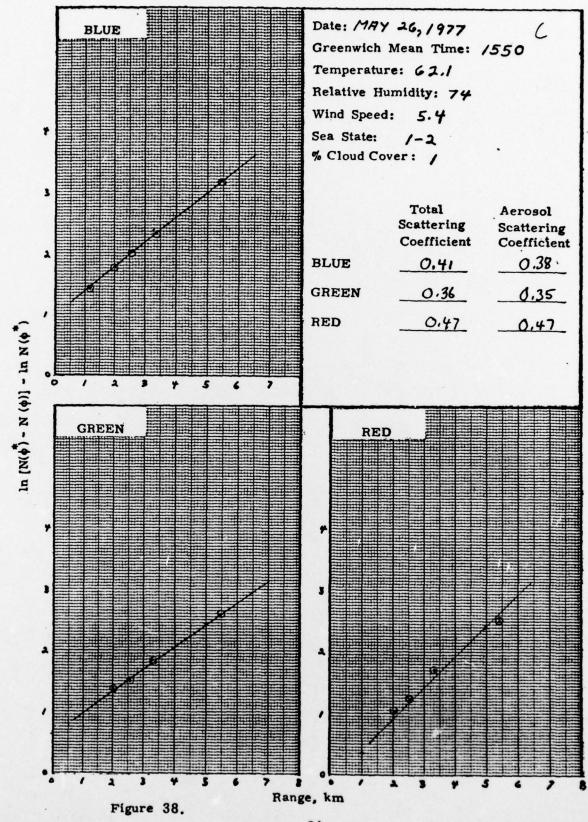
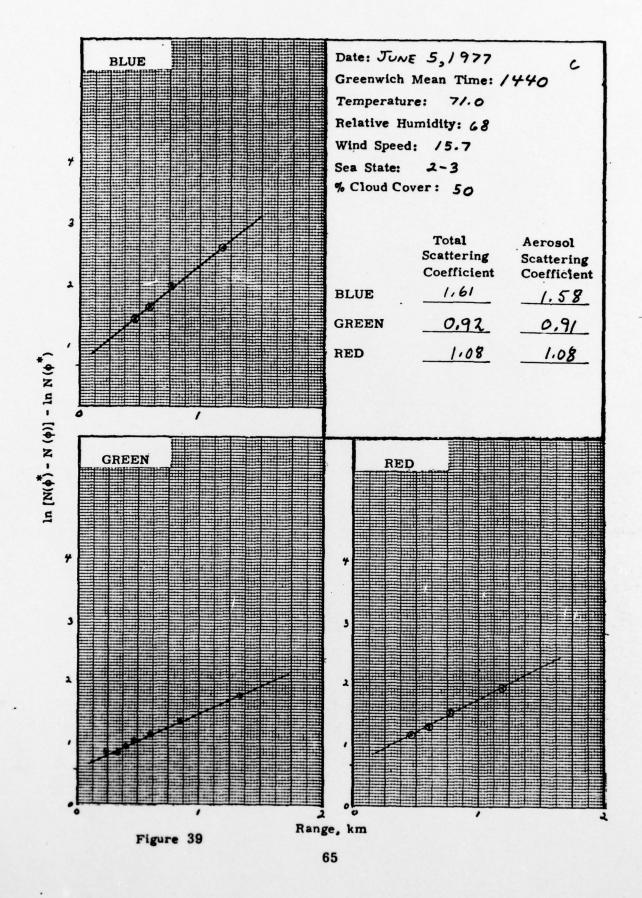


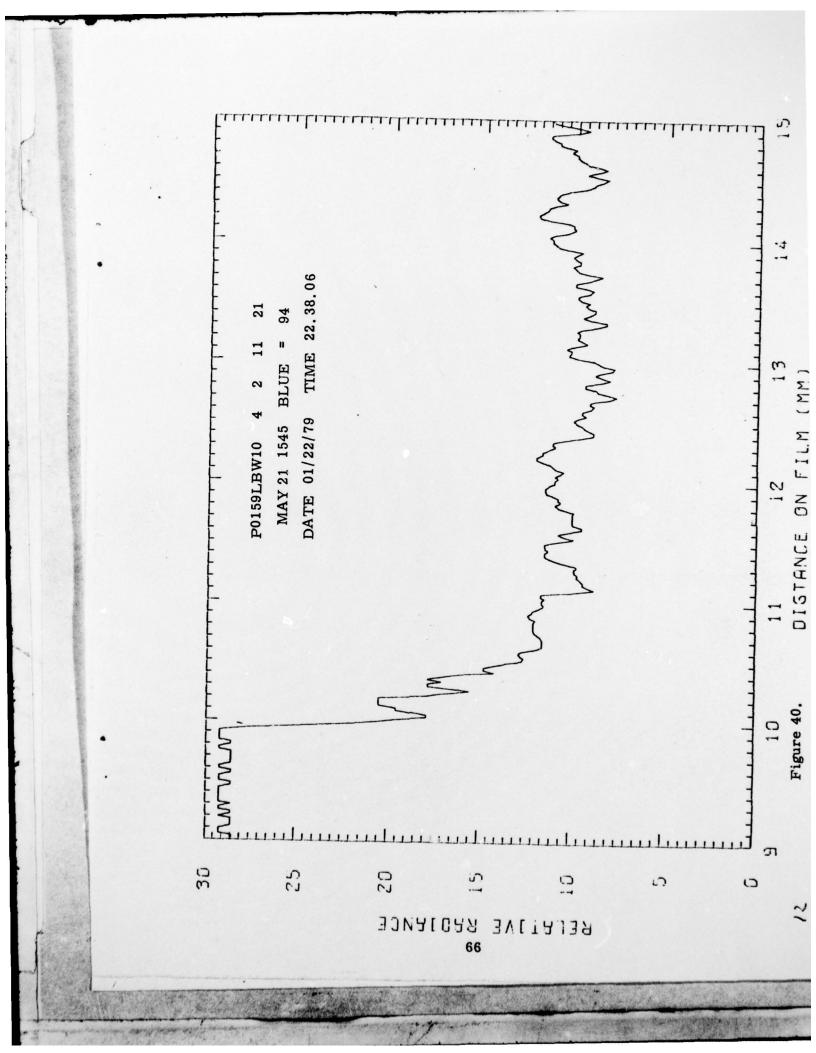
Figure 35. May 22,1977 Time 1830 EOMET FR 10 Film 6 Segment 2.











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